A simple method for EEG guided transcranial electrical stimulation without models

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Abstract

Objective. There is longstanding interest in using EEG measurements to inform transcranial Electrical Stimulation (tES) but adoption is lacking because users need a simple and adaptable recipe. The conventional approach is to use anatomical head-models for both source localization (the EEG inverse problem) and current flow modeling (the tES forward model), but this approach is computationally demanding, requires an anatomical MRI, and strict assumptions about the target brain regions. We evaluate techniques whereby tES dose is derived from EEG without the need for an anatomical head model, target assumptions, difficult case-by-case conjecture, or many stimulation electrodes.

Approach. We developed a simple two-step approach to EEG-guided tES that based on the topography of the EEG: (1) selects locations to be used for stimulation; (2) determines current applied to each electrode. Each step is performed based solely on the EEG with no need for head models or source localization. Cortical dipoles represent idealized brain targets. EEG-guided tES strategies are verified using a finite element method simulation of the EEG generated by a dipole, oriented either tangential or radial to the scalp surface, and then simulating the tES-generated electric field produced by each model-free technique. These model-free approaches are compared to a ‘gold standard’ numerically optimized dose of tES that assumes perfect understanding of the dipole location and head anatomy. We vary the number of electrodes from a few to over three hundred, with focality or intensity as optimization criterion.

Main results. Model-free approaches evaluated include (1) voltage-to-voltage, (2) voltage-to-current; (3) Laplacian; and two Ad-Hoc techniques (4) dipole sink-to-sink; and (5) sink to concentric. Our results demonstrate that simple ad hoc approaches can achieve reasonable targeting for the case of a cortical dipole, remarkably with only 2–8 electrodes and no need for a model of the head.

Significance. Our approach is verified directly only for a theoretically localized source, but may be potentially applied to an arbitrary EEG topography. For its simplicity and linearity, our recipe for model-free EEG guided tES lends itself to broad adoption and can be applied to static (tDCS), time-variant (e.g., tACS, tRNS, tPCS), or closed-loop tES.

Keywords: EEG, computational modeling, tES, evoked potentials, MRI, reciprocity

(Some figures may appear in colour only in the online journal)
in principle should reflect task/subject specific brain regions to be targeted by tES. The relationship between scalp EEG and tES is formalized by the reciprocity principle: the electrical path taken by an applied scalp current to the location of a biological current source, is symmetric to the path taken by the activation of that biological source to the (now recording) scalp electrodes (Helmholtz, 1853; Rush and Driscoll, 1969). But this theoretical principle does not directly inform a method for practical implementation. A ‘brute force’ implementation using numerical simulations of tES targeting requires anatomically specific models (subject specific scans and tissue segmentation; [2, 3]), statistical assumptions for source localization from EEG that have yet to be validated [4], and computationally intensive dose optimization for tES [5, 6]. Moreover, this workflow is subject to a hard decision (i.e., commitment to the implicated brain region) on target selection and how to quantify a ‘good’ optimization result [5]. Thus, despite highly compelling value for EEG-guided tES (see below), adoption is limited by methods that are burdensome and/or poorly constrained [1, 7, 8].

Typically when, without a model, EEG is used to identify a target [9–11] or to select tES waveform [11–13], electrodes (often large pads) are positioned based on rules-of-thumb such as placing one electrode ‘over’ the region of interest and the other one at ‘some distance’. Model-driven efforts on EEG guided tES have been considered with increasing sophistication and computational burden [7, 14, 15]. tES-EEG ‘reciprocity’ is a concept adapted from the circuit theory and requires a head model (circuit path) to specify reciprocity between each electrode and brain region [8, 16, 17].

Though a longstanding notion, recent developments make EEG guided tES more desirable and feasible. For example, despite encouraging results from human trials of tES [18–23], there are concerns about inter- and intra-individual variability [24–27]. So a need exists for methods to customize dose, ideally in a manner that is not burdensome (e.g., not neuro-navigated). Indeed, clinically effective (FDA-approved) neuromodulation technology typically requires patient-specific setup for success, including neuroanatomical TMS and DBS [28–31]; clinical adoption of tES may ultimately be supported through EEG-guidance. EEG-informed tES can be implemented under open-loop, where EEG is imaged before stimulation [32], or as closed-loop regimes given that scalp EEG patterns vary in time, and tES has been shown to modulate EEG activity [33–37]. EEG-guided tES is supported by increased sophistication in EEG and stimulation hardware [14, 15, 38]. For example, compact gel-based electrodes designed for tES (high-definition electrodes; [39, 40]) allow integration with EEG headgear (e.g., HD-tDCS, HD-tACS; [41–45]) including the reproduction of conventional pad montages [46]. What is lacking is a simple recipe for mapping EEG measurements into tES parameters.

The ideal methodological approach would: (1) not require subject specific imaging (not neuro-navigated [47]; (2) automatically adapt to any EEG electrode deployment (e.g., 10-10, concentric, custom) and inject current through the same electrodes (positions); while (3) limiting the number of electrodes used for tES, regardless of EEG density, to a selectable amount (balancing reasons to minimize stimulation channels with current per electrode); (4) account for neural source orientation as well as position [48]; while (5) naturally balancing tES optimization for focality versus intensity, which can be divergent criteria [5]; (6) be linear or otherwise apply to any static (tDCS) or time-dependent application (tACS); while (7) lending itself to various forms of EEG analysis (e.g., filtering) and decomposition [38]; (8) allow specific current limits based on tolerability and safety standards (e.g., maximum current per channel [49–51]); but notwithstanding all the above (9) remain computationally light, allowing even closed-loop applications (e.g., a dynamic EEG and tES). An approach fulfilling these criteria would be simple and broadly deployable, and thus facilitate diverse applications of EEG-guided tES—essentially in any domain where there is an EEG marker of the cognitive/behavioral target with inter-individual variability [52–57]. The model-free techniques evaluated here, and particularly the proposed approaches that select a limited number of electrodes for stimulation based on EEG features, aim to achieve these goals.

Methods

Finite element model

An exemplary [25, 58, 59] MRI-derived finite element model of a head of a subject who reported no cerebral damage was generated from a 3T MRI scan that had an isotropic 1 mm$^3$ resolution. The MRI was segmented by ScanIP software (Simpleware, Exeter, UK) which each voxel isotropic conductor volume assigned one of seven conductivities [60–68]: air (10$^{-15}$ S m$^{-1}$), bone (10$^{-2}$ S m$^{-1}$), cerebrospinal fluid (CSF), 1.65 S m$^{-1}$, fat (0.025 S m$^{-1}$), gray matter (0.276 S m$^{-1}$), skin (0.465 S m$^{-1}$), white matter (0.126 S m$^{-1}$). Dipoles are often used as representations for electrically-active patches of neuronal tissue [69–72]. We separately modeled two dipoles, one tangential and one radial to the cortex. Each dipole source was simulated by 2 voxels, negative and positive poles, separated by 1 mm. Dipoles were positioned on the left hemisphere of the somatosensory cortex, in the Brodmann area 3 over the somatotopic representation of the hand. The two dipoles patterned the cortical activation of a sensory evoked potential generated by the right median nerve stimulation [73–75].

331 high definition (HD) electrodes (disc electrodes having skin contact area of 0.8 cm$^2$ each) with realistic underlying gel (0.3 S m$^{-1}$) were projected onto the scalp surface as tissue segmentations using a previously developed Matlab script (Kempe et al 2014) [15, 25, 38, 46, 48, 58–76]. Electrodes were distributed across the scalp surface of the model (figures 1(A) and (B)) allocated according to the International 10-10 System [77] and 10-5 submultiples. It included two axial lines of electrodes below the plane of the eyes, and one electrode over the back of the neck (which was used as a reference), except avoiding regions over the orbit, ears, and nose. The scalp electrodes were used to either to (1) simulate EEG by collecting voltage over the scalp produced by brain dipoles, or (2) deliver current during tES with a set current at each electrode.
Adaptive volumetric meshing was applied to the tissue segmentation in ScanIP (Simpleware Ltd, Exeter, UK) with a compound coarseness of $-15$ (maximum edge length 1.85 mm, target minimum 0.775 mm, target Jacobian minimum 0.1). The resulting meshes consisted of $>10\,000\,000$ quadratic tetrahedral elements and $>15$ million degrees of freedom. Further refined meshes were found to have no noticeable effect on simulation results. The mesh was imported in COMSOL Multiphysics 4.3 (Burlington, MA) to simulate quasi-static volume conductor physics. The quasi-static approximation is considered reasonable for both EEG and tES [67, 78–81]. Within COMSOL, the Laplace equation ($\nabla \cdot (\sigma \nabla V) = 0$, $\nabla \cdot$ : divergence; $\nabla$ : gradient; $\sigma$ : conductivity; $V$ : electric potential) was solved for voltage distribution given distinct Dirichlet or Neumann boundary conditions depending on EEG or tES simulation. COMSOL implemented a linear system solver of conjugate gradients with a relative tolerance of $1 \times 10^{-6}$.

**tES simulation: electrode activation**

When current stimulation was applied in the tES condition, a boundary condition of normal current density was implemented to each stimulating electrode. For each electrode, the current value was divided by the skin-electrode contact area and was applied as current density boundary condition and assigned to the mesh nodes as current loads representing the right-hand-side of the linear system of equations.

**EEG simulation: brain source activations**

An electric potential of 1 mV, with boundary conditions $-0.5$ mV at the negative pole and $+0.5$ mV at the positive one, was applied to the brain sources for each dipole direction. The positive pole was chosen to point towards the frontal lobe for the tangentially-oriented dipole, and the positive pole toward the scalp surface for the radially-oriented dipole. For the EEG simulation, to obtain a correct scalp voltage distribution, the conductivity of the HD electrodes over the scalp surface was set $\sigma = 10^{-9}$ (e.g., analogous to electrodes connected to a high impedance EEG amplifier). The computed voltage was sampled from the electrode center. Such value, because of the small electrode size, showed, indeed, negligible difference with the averaged voltage under the electrode’s surface. We simulated the EEG potentials from 330 electrodes with the neck electrode being the reference [82]. The dipole models produced two different characteristic scalp voltage distributions ([73–75]; figure 2, top).

In some cases, voltage only sub-multiples or Ad-Hoc electrodes were used to determine tES dose (see electrode montage selection).

**Model-free approaches**

The central objective of this paper is to evaluate various approaches for tES based on EEG without the dependence on a head model. A head model was however employed to emulate an exemplary EEG and to verify the performance of these approaches only in the evaluation of this paper. We emphasize that the steps that generate the information guiding tES are model-free. For our model-free processes (table 1) we distinguish between two methods: (A) EEG-to-tES mapping techniques, where the voltage or current applied to each tES electrode is determined; and (B) electrode montage selection, where the number and location of electrodes used for tES is determined—sampled from the electrodes used for EEG.
EEG-to-tES mapping technique is thus only applied to the set of tES electrodes selected.

**EEG-to-tES mapping technique.** This section addresses assignment of stimulation voltage or current to the pre-selected electrodes for five model-free approaches. In three approaches the current applied is calculated from the simulated EEG: ‘voltage-to-voltage’, ‘voltage-to-current’, and ‘Laplacian’. For these approaches either uniform or Ad-Hoc tES electrode selection (see ‘tES electrode montage selection’ paragraph) can be applied. For the remaining two approaches ‘sink-to-sink’ and ‘sink-to-concentric ring’, the current values applied were not

![Figure 2](image_url)
calculated from the EEG information, but electrode selection was EEG guided using the Ad-Hoc tES electrode selection.

**Voltage-to-voltage.** This is a basic EEG-to-tES mapping technique in which the voltage EEG values are applied to the stimulating electrodes. For each channel:

$$\Delta V_{1\text{stim}} = -\frac{\Delta V_{1\text{EEG}}}{\Delta V_{1\text{tot}}} \cdot \Delta V,$$

$$\Delta V_{\pi\text{stim}} = -\frac{\Delta V_{\pi\text{EEG}}}{\Delta V_{\pi\text{tot}}} \cdot \Delta V.$$

To apply a zero average stimulation of 1 mV, the potential of each electrode ($\Delta V_{1\text{stim}}$) was divided by the sum of all the potentials with the same polarity ($\Delta V_{1\text{EEG}}$) and then multiplied by $\Delta V = 0.5$ mV. Uniform and Ad-Hoc positioning were applied.

**Voltage-to-current.** The zero average referenced values (see voltage-to-voltage section) were applied to the electrodes as

$$I_{1\text{stim}} = -\frac{\Delta V_{1\text{EEG}}}{\Delta V_{1\text{tot}}} \cdot I,$$

$$I_{\pi\text{stim}} = -\frac{\Delta V_{\pi\text{EEG}}}{\Delta V_{\pi\text{tot}}} \cdot I,$$

where $I_{1\text{stim}}$ is the current intensity applied at each electrode and $I$ is the total current delivered through all the electrodes. In all the simulations total current was set $I = 1$ mA ($+1$ mA of total anodic and $-1$ mA of cathodic current intensity). Uniform and Ad-Hoc positioning were applied.

**Laplacian.** The Laplacian operator was applied to the EEG values. Surround electrodes were defined as those centered within a 3 cm radius of the evaluated electrode channel. In this way, we obtained a complete ring of electrodes around each channel to estimate the average to subtract. In the case that one electrode was not circumscribed by a complete ring of electrodes, it was excluded from the stimulation. Potentially, for the Laplacian montage, if information about the cortical region involved in the source activation is known, as it is during an evoked potential EEG, a different weight among the channels can be applied to increase the focality of

<table>
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<td>5 (4 X 1), 6 (4 X 2), 6 (5 X 1)</td>
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<tr>
<td></td>
<td>Model Based</td>
<td>N/A</td>
<td>8 (4 X 4), 2 (1 X 1)</td>
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the Laplacian EEG-to-tES mapping technique

\begin{align*}
I_{\text{stim}}^{i} &= - \frac{\Delta V_{i}^{\text{EEG}}}{\Delta V_{\text{tot}}^{\text{EEG}}} \cdot \sum_{i=1}^{n} w_{i} \cdot \frac{\Delta V_{i}^{\text{EEG}}}{n} \cdot I, \\
I_{\text{stim}}^{n} &= - \frac{\Delta V_{n}^{\text{EEG}}}{\Delta V_{\text{tot}}^{\text{EEG}}} \cdot \sum_{i=1}^{n} w_{i} \cdot \frac{\Delta V_{i}^{\text{EEG}}}{n} \cdot I.
\end{align*}

The weight \( w \) was set as a unitary vector for all the channels to not introduce difference in evaluating the different approaches.

The obtained values were zero averaged and normalized to deliver 1 mA of total current intensity for all the selected montages. Uniform and Ad-Hoc positioning were applied.

**Sink-to-sink.** This is a \( 1 \times 1 \) configuration, having one anode and one cathode. The boundary condition of 1 mA was set for the anode, while the cathode was set as ground (effectively collecting \(-1 \) mA).

**Sink-to-ring.** Concentric ring electrode configurations were applied using 1 mA for the central cathodes and setting the anodes as ground.

**tES Electrode montage selection.** The EEG-to-tES mapping approaches evaluated in this work were applied using two general approaches to select number and location of tES electrodes: those based on uniform distribution and those based on EEG guided Ad-Hoc selection (table 1).

**Uniform.** In this case either the entire set of 330 electrodes is used, which were distributed using the International Systems EEG positioning (see above) or uniform sub-multiples: 256, 128, 64, 32, 16, 8 electrodes. Uniform selection is independent of the EEG generated. The current applied to each electrode in the uniform set is always based on the EEG (see EEG-to-tES mapping techniques) but we emphasize that the selection of electrodes for the uniform case is not based on the EEG.

**Ad-Hoc.** This electrode selection is based on specific EEG topographies. Two general approaches are used to select tES electrodes based on the EEG: either electrodes are selected by maximum/minimum EEG voltage or maximum/minimum EEG Laplacian. While the EEG voltage and Laplacian are calculated as described in the sections above, it is important to distinguish between the use of this information to select electrodes in this section, with the subsequent use of this information to determine applied current at selected electrodes. The methods for selecting number of electrodes based on Ad-Hoc approaches available for tES are described below and vary from 2 to 8. For the different Ad-Hoc techniques, the current applied at each electrode may or may not be calculated from the EEG, depending on the approach:

- \( 1 \times 1 \) (2 electrodes), one anode and one cathode were selected as the EEG electrodes with minimum and maximum (bipolar distribution case) voltages (Ad-Hoc voltage) or Laplacian (Ad-Hoc Laplacian). The sink-to-sink mapping technique was applied to this montage, which reproduces a bipolar distribution and where the applied current does not depend on the EEG.
- \( 2 \times 2 \) (4 electrodes) two anodes and two cathodes were selected as the EEG electrodes with the two minimum and maximum values (bipolar distribution case) of voltage (Ad-Hoc Voltage) or Laplacian (Ad-Hoc Laplacian). The Voltage-to-Current and Laplacian approaches were applied to this montage, which reproduces a bipolar distribution and where the applied current depend on the EEG.
- \( 4 \times 4 \) (8 electrodes) four anodes and four cathodes were selected as the EEG electrodes with the four minimum and maximum values (bipolar distribution case) of voltage (Ad-Hoc Voltage) or Laplacian (Ad-Hoc Laplacian). The voltage-to-current and Laplacian techniques were applied also to this montage, which reproduces a bipolar distribution and where the applied current depend on the EEG.

**Model-based approaches.** Model-based approaches were implemented here only as performance references against the model-free approaches (table 1). The method to rigorously optimize tES based on a known head model and target, and with arbitrary constraints on number of electrodes and electrode currents, was previously described \([5]\) and reproduced here allowing the use of either 8 electrodes, for targeting based optimization, or 2 electrodes, for intensity based optimization. We have previously shown that this form of electrode number restriction will not significantly reduce performance based on the optimization criterion \([5, 62]\).

**Scalp potentials generated by tES.** In each stimulation case, we predicted the voltage generated on the scalp by the stimulation. By contrasting this with the scalp potentials generated by the dipole sources, we are able to ask if and how homology between tES indicted scalp potential and EEG influences resulting performance.
Quantitative performance analysis. We considered the following parameters to quantify the dose delivered into the brain:

- **Intensity**: the criterion of intensity for each stimulation was identified as the electric field (EF) magnitude generated in the central voxel of the source location. Since the total current was fixed in all cases (1 mA) this allowed comparison of intensity optimization at the target location across montages.

- **Focality**: we considered the ratio between the EF Magnitude at the target location and the mean electric field across the gray matter (mean EF magnitude, voxel wise average cross gray matter), an index of stimulation focality.

- **Directionality**: for all the model solutions we calculated the angle between the $\vec{E}F$ generated by tES and dipole source vectors

  \[
  \text{Tangential: } \theta(\vec{E}F, \vec{s}_{\text{tangential}}) = \theta(\vec{E}F, \vec{e}_x) = \arccos \left( \frac{\Delta y_{\vec{E}F}}{\pm \sqrt{\Delta x_{\vec{E}F}^2 + \Delta y_{\vec{E}F}^2 + \Delta z_{\vec{E}F}^2}} \right) \\
  \text{Radial: } \theta(\vec{E}F, \vec{s}_{\text{radial}}) = \theta(\vec{E}F, \vec{e}_z) = \arccos \left( \frac{\Delta z_{\vec{E}F}}{\pm \sqrt{\Delta x_{\vec{E}F}^2 + \Delta y_{\vec{E}F}^2 + \Delta z_{\vec{E}F}^2}} \right)
  \]

**Results**

**EEG Simulation**

To subsequently inform tES, scalp potentials were simulated using either a tangentially-oriented (parallel to the scalp surface) or radially-oriented (normal to the scalp surface) dipole (figure 2, top). The first one produced a dipolar scalp distribution, positive on the frontal section of the scalp and negative on the back of the head, with the zero isopotential line crossing the scalp over the source location. The second one generated a monopolar distribution having the maximum over the dipole on the scalp surface.

**EEG guided tES using 330 channels, radially or tangentially-oriented source dipole**

We first evaluated EEG-guided tES approaches that utilize the maximum number of available electrodes, under an *a priori* assumption that leveraging more electrodes might enhance performance in EEG-guided tES targeting. In these cases, the tES electrode montage was uniform using 330 electrodes (see methods). Three tES EEG-to-tES mapping techniques (the method which determines the voltage or current set at each electrode based on the EEG signal) were evaluated: voltage-to-voltage (330 electrodes), voltage-to-current (330 electrodes) and ‘Laplacian’ (290 electrodes as edge electrodes are not available in this case). These model-free approaches were compared to two model-based approaches: optimization of intensity using 2 electrodes, and optimization of focality using 8 electrodes. In every case we evaluated performance for a dipolar source, tangentially (figure 2, left column) or radially (figure 2, right column) oriented and quantified the maximum electric field generated in the brain (max EF magnitude), the electric field magnitude at the dipole target (target EF magnitude), the mean electric field across the gray matter (mean EF magnitude), and the orientation of the electric field at the position of the dipole relative to the dipole (directionality). We also determined the scalp voltage generated by the tES montage in order to quantify homology between the EEG potentials and the voltage in the EEG informed tES.

For the tangentially-directed dipole, all five approaches (three model-free, and two model-based) generated a dipolar distribution on the scalp; for model-free approaches the distribution matched the EEG topography (figure 2), while for model-based approaches it was localized (figure 2). We note that when the distribution of the voltage generated on the scalp by tES matches the EEG topography, the resulting brain current flow is (1) not necessarily targeted with higher accuracy than montages which generate different scalp voltage distribution (2) not necessarily consistent across tES approaches (focality: voltage-to-voltage 0.89, voltage-to-current 1.24, Laplacian 1.92, model-based 2.54 and 2.89; see figure 2 for the scalp voltage distributions and figure 6 for the parameter comparison). For example, the Voltage-to-Voltage approach generated scalp voltages comparable to the EEG, but produces a current flow in the brain that does not affect the target with focality comparable to the other techniques (figure 2, left, row 2). The voltage-to-voltage approach is not further considered. The voltage-to-current and Laplacian techniques both produced current intensity at the target that is close to the maximum brain current intensities and an orientation at the target close to the dipole (figure 2, left). We predicted moderately better focality for the Laplacian approach. Both approaches diffused current in the right hemisphere, anteriorly and posteriorly to the central sulcus, in spite of the target location being in the left somatosensory cortex (figure 2). Given these encouraging results, the need for a high number of electrodes are later considered for the voltage-to-current and Laplacian techniques. The model-based approaches (figure 2, left, bottom two rows) demonstrate higher focality or intensity values, according to the intensity (focality 2.54, intensity 1.22 V m$^{-1}$) or focality (focality 2.89 and intensity 1.07 V m$^{-1}$) optimizations. So intensity optimization enhances electric field at the target (14%), while focality optimization minimized mean electric field outside the target (relative to the target electric field, 13%).

For the radially-oriented dipole, the model-free approach using 330 electrodes performed less well than the tangential case. Voltage-to-voltage did not generate an electric field centered at the target location but in the left temporal region (intensity 0.17, focality 1.54; figure 2, right column, second row). Voltage-to-current showed slightly better relative performance concerning Intensity and slightly worse regarding focality (intensity 0.17, focality 1.11; figure 2, right column, third row). Both these tES approaches generate a unipolar scalp voltage distribution comparable to the EEG. The Laplacian approach generated a bipolar voltage distribution with a negative pole centered on the frontal area of the scalp, absent in the EEG, and
a current flow anterior to the target. These approaches were not considered further. The model-based approaches (figure 2, right, bottom two rows) demonstrate higher focality or intensity values, either for the case of intensity (focality 1.43 and intensity 0.93 V m\(^{-1}\)) or focality (focality 3.94 and intensity 0.75 V m\(^{-1}\)) optimizations. So the intensity optimization enhances electric field at the target but polarizes much of the hemisphere (figure 2, second-last row). Focality optimization is only moderately targeted (figure 2, last row).

In summary, carrying out computational modeling of EEG guided tES, we found no evidence the tES approaches that produce scalp voltages that replicate the EEG or provide enhanced brain targeting. The performance of various EEG-to-tES mapping approaches may depend on the general features of the scalp EEG (dipole or unipolar distribution) such that we continue to separately consider the radial and tangential source cases—including when we propose Ad-Hoc approaches. When \(\sim300\) electrodes are used, Laplacian mapping, followed by voltage-to-current generate better performance than voltage-to-voltage. We next consider the role of electrode number.

**EEG guided tES using sub-set of uniform-distributed channels, tangentially-oriented source dipole**

For the case of a tangentially-orientated dipole, we further considered the voltage-to-current and Laplacian techniques, reducing the number of tES electrodes from 256, to 128, to 64, to 32, to 16, and to 8 (figure 3). We emphasize that these electrode montages were always uniform, and electrode selections were not informed by the EEG (in contrast to Ad-Hoc approaches). We observed that focality decreases dramatically as electrode number is reduced below 32 for the voltage-to-current method and below 64 for the Laplacian method (figures 3, 4 and 6).

We therefore conclude that for the most promising uniform electrode montage approach, a relatively high number of electrodes are needed. Yet, model-based approaches suggest that optimized performance can be obtained with a low number of electrodes (figure 2, bottom two rows; [5, 62]). These results encouraged us to consider non-uniform based electrode montage based on Ad-Hoc selection next.

**EEG guided tES using an Ad-Hoc selection of channels, tangentially and radially-oriented source dipole**

With our Ad-Hoc technique, the selection of electrodes (see sink-to-sink and sink-to-ring paragraphs in the EEG-to-tES mapping techniques section) is based on the EEG.

For the case of a tangentially-oriented dipole (bipolar EEG) we considered an electrode montage selection process based on selecting the electrode with the highest EEG voltage (figure 5, first column) or highest EEG Laplacian (figure 5, second column). When electrodes were selected based on voltage, voltage-to-current was used to determine tES electrode current. When electrodes were selected based on EEG Laplacian, Laplacian technique was used to determine tES electrode current. In each case we considered a selection of 8, 4, or 2 electrodes for tES, with 1 mA distributed across all electrodes. In the case of 2 electrodes (bottom row), the current applied to the electrodes was fixed at 1 mA, so the technique is sink-to-sink. Interestingly, all Ad-Hoc approaches that were tested (figure 5) showed a better combination between intensity and focality (figure 6, top) than the one obtained with the uniform electrode montages (figure 2). Thus using less electrodes (2–8) but selecting electrodes based on the EEG (figure 5), enhances performance. Moreover, for both Ad-Hoc approaches, reducing the number of electrodes from 8 to 2 where cathode and anode are placed in the location of the absolute maximum and minimum (sink-to-sink technique), enhanced performance in regards to intensity, focality and orientation (figures 5 and 6). For sink-to-sink (using just two electrodes) Laplacian EEG based electrode selection (intensity 1.14 V m\(^{-1}\), focality 5.18) produced slightly lower peak at the target with improved focality compared to EEG voltage based electrode selection (intensity 1.21 V m\(^{-1}\), focality 2.75).

For the case of radially-oriented dipole (unipolar EEG) we considered an electrode montage selection process based on selecting an electrode with the highest EEG voltage (figure 5, third columns) or electrodes with the highest EEG Laplacian (figure 5, fourth column). When electrodes were selected based on EEG voltage, a ring montage was used with 1 mA applied to the center electrodes. When electrodes were selected based on EEG Laplacian, Laplacian technique was used to determine tES electrode current—an identical method as for the tangential case. Again, we discovered that using less electrodes but selecting electrodes based on the EEG (4 × 1: focality 4.4, intensity 0.31 V m\(^{-1}\), directionality 9°; figure 5) resulted in a dramatic increase of focality compares to approaches using even hundreds of electrodes (voltage-to-current technique with 256 electrodes: focality 1.6, intensity 0.54 V m\(^{-1}\); figure 2). The concentric ring montage produced the best targeting; performance was already optimal with 4 × 1 (focality 4.4) such that adding more electrodes, either cathodes or anodes, did not significantly change brain current flow (5 × 1: focality 4.0, intensity 0.32 V m\(^{-1}\), directionality 9°; 4 × 2: focality 4.40, intensity: 0.31 V m\(^{-1}\), directionality 9°; figure 5). In comparison, the Laplacian method was less focal when applying 8 electrodes (focality 2.30, intensity 0.62 V m\(^{-1}\), directionality 34°), and performance even degraded as the number of electrodes decreased (4 electrodes: focality 2.30, intensity 0.31 V m\(^{-1}\), directionality 26°; 2 electrodes: focality 1.5, intensity 0.12 V m\(^{-1}\), directionality 22°; figure 5).

In summary, we report that the Ad-Hoc approach improves performance over uniform electrode montage, and in contrast to uniform electrode montage, requires fewer electrodes (2–8 depending on approach). In the case of bipolar EEG, Laplacian electrode selection with two electrodes (Sink-to-Sink) is superior based on brain targeting/intensity and low-electrode count among Ad-Hoc approaches tested. Similarly, in the case of unipolar EEG, concentric ring with 4 × 1 montage is superior. The Laplacian Ad-Hoc method (Laplacian electrode and current selection) with 8 electrodes is the most robust approach across methods in which the current was based on the EEG.

**Overall performance comparison with model-free uniform electrode, model-free Ad-Hoc, and model-based techniques**

Overall performance was compared across all tested montages quantifying intensity at target versus focality, as this represent
a fundamental trade-off in tES [5]. For a tangentially-directed dipole, two model-free Ad-Hoc approaches with just 2 electrodes produced maximum target intensity compared to model-based optimization: the montages with sink-to-sink current application, having electrodes selected in function of the EEG voltages (intensity 1.21 V m$^{-1}$, focality 2.75; figure 5) and the Laplacian (intensity 1.14 V m$^{-1}$, focality 5.18; figure 5). The latter with slightly less target intensity but

Figure 3. Voltage-to-current and Laplacian EEG-to-tES mapping techniques. Tangential comparison using uniform electrode montages.
almost double focality. The improved focality compared to model-based focality optimization should be understood as reflecting a difference in how focality is scored; model-based approaches guarantee best performance given a specific cost function [5]. Approaches with uniform electrode montage generally underperformed; among them Laplacian current application with 64 or greater electrodes produced reasonable focality (focality ~ 2.5) and around half intensity (0.52, 0.50 and 0.53 V m⁻¹) of the sink-to-sink Ad-Hoc approaches (1.14 and 1.21 V m⁻¹).

For a radially-directed dipole, the model-free Ad-Hoc ring based approach resulted in focality around ten times higher (focality ~40) than other approaches (max focality 4 for the model-based approach). Here again improvement against model-based focality optimization should be read as based on the cost function which provided the numerical optimization [5, 6]. Model-based tES also produced higher intensities at the target. The Ad-Hoc Laplacian based method with 8 electrodes was the closest performance (intensity 0.62 V m⁻¹, focality 2.3) to model-based optimization (intensity 0.75 V m⁻¹, focality 3.9).

**Discussion**

Our approach for model-free targeting of tES by EEG was previously presented in abstract form [85].

The theoretical benefit to leveraging EEG to guide tES is entirely dependent on the strategy (methodological approach) used and constraints on the stimulation technology (pad versus HD style electrode, 2 electrodes versus arrays; [86]) as well as the nature of the EEG. Through a computational analysis, this paper develops a first step toward strategies for EEG guided tES expressly to exclude models, based on examples from single dipoles. We demonstrate remarkable overall brain targeting performance with model-free approaches that require few (2–8) electrodes. Our novel Ad-Hoc approaches are optimized based on distinguishing two typologies of scalp EEG distributions: monopolar as in the radially-oriented dipole and bipolar as in the tangentially-oriented dipole; the former indicating a tES concentric ring approach targeted around EEG voltage minimum and the latter a tES sink-to-sink targeted around the EEG Laplacian (figure 5). Alternatively, without distinguishing these general EEG distributions, tES based on EEG Laplacian with 8 electrodes provides high performance (figure 5, right). Our results cast doubt on the notion that an optimal tES strategy should provide a scalp voltage distribution that approximates the EEG (e.g., voltage-to-voltage shows high homology between EEG and tES scalp voltage but poor targeting, figure 2). And our results show that many (hundreds) of tES electrodes are not necessarily needed if the right strategy is used (compare performance reliance on high electrode number with uniform approaches in figure 3 with low electrode number for Ad-Hoc approaches in figure 5). Additional features of our approach are discussed.

The goal of using EEG to design and optimize tES is not new and it is based on the reciprocity application [1]. But the adoption remains investigational [7, 8, 14, 38] and limited (see introduction, [9–13, 87]).

We discuss model-free approaches in regards to features that support adoption:

1. No need for subject-specific imaging.
2. Applicable with any EEG montage.
3. Limiting the number of stimulation electrodes to the extent desired.
4. Account for brain neural source orientation as well as position.
5. Balance tES optimization for focality versus intensity.
6. Apply to any static (tDCS) or time-dependent application (tACS, tRNS, tPCS).
7. Lend itself to various forms of EEG analysis.
8. Allow current limits based on tolerability standards.
9. Remain computationally light.

Methods that require subject-specific anatomical imaging are burdensome [2, 88, 89]. The acquisition of sufficiently precise imaging data is costly and often impractical. Subject specific imaging implies methods to model the head, which requires algorithms for tissue segmentation [90], as well as forward and/or inverse current flow simulations. Because of uncertainty, these models rely on assumptions about tissue segmentation and conductivity, the nature of brain electrical sources, etc. Even if a standard template head is used (ICBM152; New York Head; [25, 91]) the inverse problem
Figure 5. Minimal functional sets of HD electrodes. For both the dipole directions, tangential and radial, groups of two, four and eight HD electrodes were placed over the peaks of the scalp voltage distribution generated by the source (voltage peaks) and over the peaks of the Laplacian distribution (Laplacian peaks).
which relates EEG potentials to anatomical tES targets is ill-posed and thus may yield inaccurate solutions [92–95]. A method to guide tES by EEG without the need for a head model would accelerate adoption and would hopefully lead toward more clinically efficacious treatments. Yet research suggests both interpretation of EEG and design of tES [25, 91] benefit from subject specific head models. Model-free EEG guided tES is a physiological, data-driven technique that attempts to circumvent these problems by exploiting the fact that information about head anatomy and source

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**Figure 6.** Tangential and radial EEG-to-tES mapping cases chart. Scatter plot showing a quantitative tangential and radial montage comparison. Value of the electric field in the source location on the X axis and an index of focality on the Y axis, calculated as the ratio between the value of the electric field in the source location and the total electric field delivered into the gray matter. In the legend of the chart, colors mean the positioning of the electrodes and the EEG-to-tES mapping method applied to set the current intensity at each electrode. The shape of the symbols indicate the number of electrodes used in each stimulation.
orientation is intrinsically present in the EEG measurement. Leveraging this information may obviate the need for an MRI-based head model.

Various EEG electrode deployments are used, ranging from the common 10/10 and 10/20, to concentric rings, to custom configurations [93, 96–98]. These configurations are based on set-up expediency and in practice placements are approximated (e.g., using pre-loaded caps). A method that is specific to one configuration or requires registering each electrode location with a model of the head is impractical. Our approaches for model-free EEG guided tES inherently configures to any EEG deployment, even if arbitrary.

Decreasing the number of tES channels increases practicality [99]. In addition to reduced hardware complexity, whereas a few non-ideal EEG electrodes do not necessarily compromise an entire recording, for tES even one poor electrode contact can compromise tolerability [40, 77, 100]. In contrast to EEG, where broad coverage and high density enhances imaging [36, 83], for tES low-electrode deployments can approach optimality if the target is known (model-based approaches in figure 2; [5, 62, 101]). Whereas approaches based on uniform tES electrode configuration quickly degrade in performance with reduced number of electrodes (figure 3), we show that Ad-Hoc approaches achieve reasonable results by targeting with just two and five electrodes for tangential and radial modeled source directions, respectively (figure 5).

Previous studies showed how tES montages using two HD electrodes and a concentric-ring HD (e.g., 4 × 1) montage can produce targeted tangential and radial brain current flow, respectively [62, 63]. Here we suggest Ad-Hoc approaches to select and configure these tES montages guided by the EEG, and show performance approaching with the model-based optimization (figure 5). The applied tES current is not only guided to the target location, but also matches the dipole orientation (directionality; figure 5; [48]). The 4 × 1 and the sink-to-sink Ad-Hoc Laplacian montages generated current flows having respectively a solid angle (directionality) of 9.3° with the radial and 7.4° with the tangential directions.

While simple to implement, the result of the Ad-Hoc model-free EEG guided tES is not trivial. tES optimization needs to balance the antagonistic constraints of intensity and focality; with head model-based approaches this requires committing to the targeted brain region a priori [5].

The presented techniques may also find application to alternating current stimulation paradigms where one aims to modulate the amplitude of an observed brain rhythm [102–105]. For example, stimulation at the low frequencies characteristic of the EEG has been shown to selectively modulate oscillatory brain activity (e.g., alpha frequency stimulation to influence alpha related activity [106, 107]). tACS has been applied at both fixed or individualized frequencies [32]. However, optimization of the placement of tACS electrodes remains largely unexplored. The approach presented here may potentially optimize the modulation of oscillatory brain activity by stimulating at sites exhibiting maximal oscillatory amplitude at the frequency-of-interest.

The EEG is inherently time variant. Our model-free techniques are based on an instantaneous representation of the scalp voltage at each electrode and may thus be applied in a time-varying manner that ‘tracks’ the dynamic EEG pattern. Moreover, the technique is compatible with numerous commonplace EEG preprocessing methods such as basis decomposition or component analysis [108–110]. For example, our approach could be applied to a particular (spatial) EEG component which is implicated in the disorder or behavior-of-interest.

The proposed model-free approaches for EEG guided tES can be implemented with any Ad-Hoc current limits applied per electrode and/or in sum (see normalization in methods). These current limits are typically based on empirical experience (what is tolerated), and historical norms [49–51].

In addition, reducing the number of tES electrodes may reduce the burden in regards to hardware and set-up, but increases current per electrode. Our Ad-Hoc approaches allow for some flexibility in this regard.

Our Ad-Hoc approaches depend on identifying a characteristic dipole signature (radially or tangentially directed) in the EEG, and we verify performance only for a single dipole case. However, the characterization of EEG assuming a dipole EEG topography is ubiquitous (though with methodological considerations: [111–114]) leveraging conventional signal processing such as averaging (repeated evoked response), filtering, ICA, etc [110, 115–117]; mapping EEG to tES parameters based on dipoles, when they are identified in the EEG, is a rational first approximation [111–114]. The robustness of the technique across brain regions remains to be verified, but bipolar and concentric ring stimulation montages are robust across underlying anatomy [45, 118]. In this sense, use of low-electrode numbers (e.g., two or five) may be a further generalization advantage over stimulation approaches relying on a high number of electrodes.

Our approach cannot overcome limitations inherent in brain neurophysiology and/or EEG that result if a diffuse source of activity and ambiguous detection. These issues have for decades motivated imaging research [119–131]. Our emphasis here is an immediately tractable and customizable approach that at improves on current efforts that use large pads and no spatial optimization. Identification of (two) EEG channels with maximum activity is common [132–134], thus the presence of multiple (dipole) sources does not diminish our protocol to target one identified source. Evidently the scalp EEG measurements vary in time, but standard time-domain signal processing can be used to select channels [108, 135–139]. Ultimately, adoption of our approach to refine clinical treatments with tES/tDCS, depends on still further assumptions such as if targeted and individualized cortical stimulation of preferred over brain-wide stimulation. For the noted limits of our approach, it is rationale, adoptable, and testable.

The proposed approach is essentially a data-driven lookup table for designing tES montages, and thus requires minimal computational resources. It is also amenable to real-time adaptive operation limited only by how fast the electrode selection can be performed; though it is critical in such cases where interactions between stimulation and recording systems (e.g., skin erythema by tES changing EEG pick-up) need to be explicitly addressed. In summary, we proposed a simple and broadly deployable method for EEG guided tES.
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COI

MB has equity in Soterix Medical Inc. The City University of New York has patents on brain stimulation with MB as inventor.

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